

KAMARAJ COLLEGE (Autonomous)

Accredited with A+ Grade by NAAC

(Affiliated to Manonmaniam Sundaranar University, Tirunelveli)

THOOTHUKUDI – 628 003

(7 Pages)

Reg. No:

Question Code No : 25000210

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UG Degree - End Semester Examinations, November 2025

Second Semester

B.Sc. MATHEMATICS

Analytical Geometry (Two & Three Dimensions)

(For those who joined in July 2024 onwards)

Time : 3 Hours

Maximum : 75 Marks

PART - A (10 × 1 = 10 Marks)

Answer ALL Questions

Choose the correct answer:

1. The lines $y = mx$ and $y = m_1x$ are conjugate diameters of

the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ then $mm_1 =$

(a) $-\frac{b^2}{a^2}$

(b) $\frac{b^2}{a^2}$

(c) $-\frac{a^2}{b^2}$

(d) $\frac{a^2}{b^2}$

2. The length of the equi conjugate diameter of the ellipse $3x^2+7y^2=21$ is
- (a) $\sqrt{20}$ (b) $\sqrt{21}$
(c) $\sqrt{10}$ (d) $\sqrt{210}$
3. The equation of the line perpendicular to the line $p = r\cos(\theta - \alpha)$ is
- (a) $p' = r\cos(\theta - \alpha)$
(b) $p' = r\cos(\frac{\pi}{2} + \theta - \alpha)$
(c) $p' = r\cos(\pi + \theta - \alpha)$
(d) $p' = r\cos(2\pi + \theta - \alpha)$
4. The eccentricity of the conic $\frac{2}{r} = 1 + \cos\theta + \sin\theta$ is
- (a) 2 (b) 1
(c) $\sqrt{2}$ (d) $\sqrt{3}$
5. The distance from the origin to the plane $6x - 3y + 2z - 14 = 0$ is
- (a) 14 (b) 2
(c) 7 (d) 6
6. The intercept on the x-axis of the plane $x + y + z = 1$ is
- (a) 4 (b) 3
(c) 2 (d) 1

7. The plane _____ is perpendicular to the line
- $$\frac{x+2}{-1} = \frac{y-3}{1} = \frac{z+4}{3}$$
- (a) $-x + y + 3z = 4$ (b) $2x - 3y + 4z = d$
(c) $-2x + 3y - 4z = 5$ (d) $x - y - 3z = d$
8. The shortest distance between two intersecting line is
- (a) 0 (b) 1
(c) ∞ (d) Positive
9. The centre of the sphere
- $$x^2 + y^2 + z^2 - 2x + 6y + 4z - 35 = 0$$
- (a) $(-2, 6, 4)$ (b) $(2, -6, -4)$
(c) $(1, -3, -2)$ (d) $(-1, 3, 2)$
10. If the distance between the centre of the sphere is equal to the sum of their radii then the two sphere touch
- (a) Internally (b) Externally
(c) Orthogonally (d) none

PART - B (5 X 5 = 25 Marks)

Answer ALL Questions choosing either (a) or (b).

Answer should not exceed 250 words.

11. (a) A tangent to the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ whose centre is C cuts the circle $x^2 + y^2 = a^2 + b^2$ at C and C'. Prove that CP and C'Q are conjugate diameter of the

ellipse.

(OR)

(b) Show that the locus of the poles w.r.t the parabola $y^2=4ax$ of the tangent to the hyperbola $x^2-y^2=a^2$ is an ellipse.

12. (a) Derive equation of a conic.

(OR)

(b) Find the equation of the normal at the point P whose vectorial angle is α .

13. (a) Find the equation of the plane passing through the points $(3, 1, 2)$; $(3, 4, 4)$ and perpendicular to the plane $5x + y + 4z = 0$.

(OR)

(b) Find the equation of the plane passing through line of intersection of the plane $x + y + z = 1$ and $2x + 3y + 4z - 7 = 0$ and perpendicular to the plane $x - 5y + 3z = 5$.

14. (a) Find the symmetrical form of equation of the line of intersection of the plane $x + 5y - z - 7 = 0$ and $2x - 5y + 3z + 1 = 0$.

(OR)

(b) Find the equation of the orthogonal projection of

the line $\frac{x-2}{4} = \frac{y-1}{2} = \frac{z-4}{3}$ on the plane $8x + 2y + 9z - 1 = 0$.

15. (a) Show that the spheres $x^2 + y^2 + z^2 + 6x + 10y + 22z = 245$ and $x^2 + y^2 + z^2 - 12x - 14y - 18z + 141 = 0$ touch each other. Find the point of contact.

(OR)

- (b) Find the equation of the sphere through the circle $x^2 + y^2 + z^2 - 9 = 0$, $2x + 3y + 4z = 5$ and the point $(1, 2, 3)$.

PART - C (5 X 8 = 40 Marks)

Answer ALL Questions choosing either (a) or (b).

Answer should not exceed 500 words.

16. (a) If α , β be the angles subtended by the major axis of an ellipse at the extremities of a pair of conjugate diameter, show that $\cot^2\alpha + \cot^2\beta$ is constant.

(OR)

- (b) If P and D are the extremities of conjugate diameter of the ellipse, then show that the locus of the midpoint of PD is $\frac{x^2}{a^2} + \frac{y^2}{b^2} = \frac{1}{2}$.

17. (a) Trace the curve $\frac{10}{r} = 3\cos\theta + 4\sin\theta + 5$.

(OR)

(b) Derive the equation of the chord of the

$$\text{conic } \frac{l}{r} = 1 + e \cos \theta$$

Joining the points whose vectorial angles are $\alpha - \beta$ and $\alpha + \beta$.

18. (a) (i) Find the equation of the plane passing through the point $(1, -2, 3)$ and the intersection of the plane $2x - y + 4z = 7$ and $x + 2y - 3z + 8 = 0$.

(ii) Find the equation of the plane passing through the point $(2, 3, -1)$ which is parallel to the plane $3x - 4y + 7z = 0$. Also measure the distance between the two planes.

(OR)

(b) Show that the origin lies in the acute angle between the planes $x + 2y + 2z = 0$, $4x - 3y + 12z + 13 = 0$. Find the plane bisecting the angle between them and point out which bisect obtuse angle.

19. (a) Find the equation of the image of the line

$$\frac{x-1}{2} = \frac{y+2}{-5} = \frac{z-3}{2} \text{ in the plane } 2x - 3y + 2z + 3 = 0.$$

(OR)

(b) Estimate the shortest distance between the lines

$$\frac{x-3}{-1} = \frac{y-4}{2} = \frac{z+2}{1} \text{ and } \frac{x-1}{1} = \frac{y+7}{3} = \frac{z+2}{2}.$$

20. (a) A plane passes through the fixed point (a,b,c) and cuts the axes in A,B,C respectively. Show that the locus of the centre of the sphere passing through the points O,A,B,C is

$$\frac{a}{x} + \frac{b}{y} + \frac{c}{z} = 2.$$

(OR)

(b) Show that the plane $2x-y-2z=16$ touches the sphere $x^2+y^2+z^2-4x+2y+2z-3=0$. Find the point of contact.