(7 pages)

Reg. No. :

Code No.: 7388

Sub. Code: ZPHM 12

M.Sc. (CBCS) DEGREE EXAMINATION, NOVEMBER 2024.

First Semester

Physics - Core

MATHEMATICAL PHYSICS - I

(For those who joined in July 2021 & 2022 only)

Time: Three hours

Maximum: 75 marks

PART A — $(10 \times 1 = 10 \text{ marks})$

Answer ALL questions.

Choose the correct answer:

- If a set of vectors spans a vector space and is linearly independent, what is it called?
 - (a) Subspace
 - (b) Basis
 - (c) Orthogonal set
 - (d) Linear transformation

- 2. Which of the following statements about linear independence is true?
 - (a) A set of vectors is linearly independent if one vector is a scalar multiple of another
 - (b) A set of vectors is linearly independent if the only linear combination that equals the zero vector is the trivial one
 - (c) A set of vectors is linearly independent if they are all orthogonal to each other
 - (d) A set of vectors is linearly independent if their sum is the zero vector
- 3. Which of the following statements about Legendre's differential equation is true?
 - (a) It is a linear ordinary differential equation
 - (b) It has no singularities within its domain
 - (c) Its solutions are always convergent for all x
 - (d) It is a second-order differential equation
- The solutions to Legendre's differential equation are commonly referred to as:
 - (a) Bessel functions
 - (b) Hermite polynomials
 - (c) Legendre polynomials
 - (d) Laguerre functions

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- 5. Which physical principle governs the Heat Flow Equation?
 - (a) Conservation of mass
 - (b) Conservation of energy
 - (c) Conservation of momentum
 - (d) Conservation of charge
- 6. Which method is commonly used to solve the Heat Flow Equation numerically?
 - (a) Finite difference method
 - (b) Laplace transform method
 - (c) Finite element method
 - (d) Fourier transform method
- 7. What does the rank of a tensor represent?
 - (a) The number of indices in the tensor
 - (b) The number of components in the tensor
 - (c) The number of dimensions in the space the tensor acts upon
 - d) The order of the tensor

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- 8. What is the contraction of a tensor?
 - (a) The operation of raising the indices of a tensor
 - (b) The operation of lowering the indices of a tensor
 - (c) The operation of summing over repeated indices in a tensor product
 - (d) The operation of multiplying two tensors together
- 9. What is the mean of a binomial distribution?
 - (a) np

(b) nq

(c) p/q

- (d) p+q
- 10. Which of the following statements is true regarding the shape of the binomial distribution?
 - (a) It is always symmetric
 - (b) It is always positively skewed
 - (c) It is always negatively skewed
 - (d) Its skewness depends on the values of n and p

PART B —
$$(5 \times 5 = 25 \text{ marks})$$

Answer ALL questions, choosing either (a) or (b). Each answer should not exceed 250 words.

11. (a) State and prove expansion theorem.

Or

(b) Show that the vectors (1,2,-3)(1,3,-2) and (2,-1,5) are linearly independent.

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[P.T.O.]

12. (a) Prove that $x L_n(x) = n L_n(x) - n L_{n-1}(x)$.

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- (b) Prove that $P_n(x) = \frac{1}{2^n n!} \frac{d^n}{dx^n} (x^2 1)^n$.
- (a) Obtain the solution of Laplace's equation in Cartesian coordinates.

Or

- (b) Explain 'D' Alembert's solution in partial differential equation.
- (a) Define contravariant, covariant and mixed tensors. Give examples.

Or

- (b) Explain the addition and subtraction of tensors.
- 15. (a) Find the correlation coefficient from the following data.

Or

(b) The following data are the number of seeds germinating out of 10 on damp filter for 80 sets of seeds. Fit a Binomial distribution to these data.

x 0 1 2 3 4 5 6 7 8 9 10 f 6 20 23 12 8 6 0 0 0 0 0

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PART C — $(5 \times 8 = 40 \text{ marks})$

Answer ALL the questions, choosing either (a) or (b). Each answer should not exceed 600 words.

(a) State and explain Gram Schmidt's orthogonalization process.

Or

- (b) State and prove Stockes theorem in vector analysis.
- 17. (a) Obtain the series solution of Laguerre's differential equation $xy'' + (1-x)y' + \lambda y = 0$.

Or

- (b) S[how that $\int_{-1}^{1} P_n(x) P_m(x) dx = \frac{2}{2n+1} \delta_{mn}$.
- (a) Obtain the Fourier series solution using method of separation of variables.

Or

- (b) Derive the equation of motion for the vibrating string.
- (a) Discuss the applications of tensor analysis for invariance of Maxwell's equations.

Or

(b) Discuss the applications of tensor analysis in electro magnetic theory.

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 (a) Ten students got the following percentage of marks in Economics and statistics.

Roll. no

1 2 3 4 5 6 7 8 9

Marks in Economics 78 36 98 25 75 82 90 62 65

Marks in Statistics 84 51 91 60 68 62 86 58 53

Calculate the coefficient of correlation.

Or

(b) Find the first four moments of the Binomial distribution.

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